



CStar: Unifying Programming and Verification in C

Di Wang

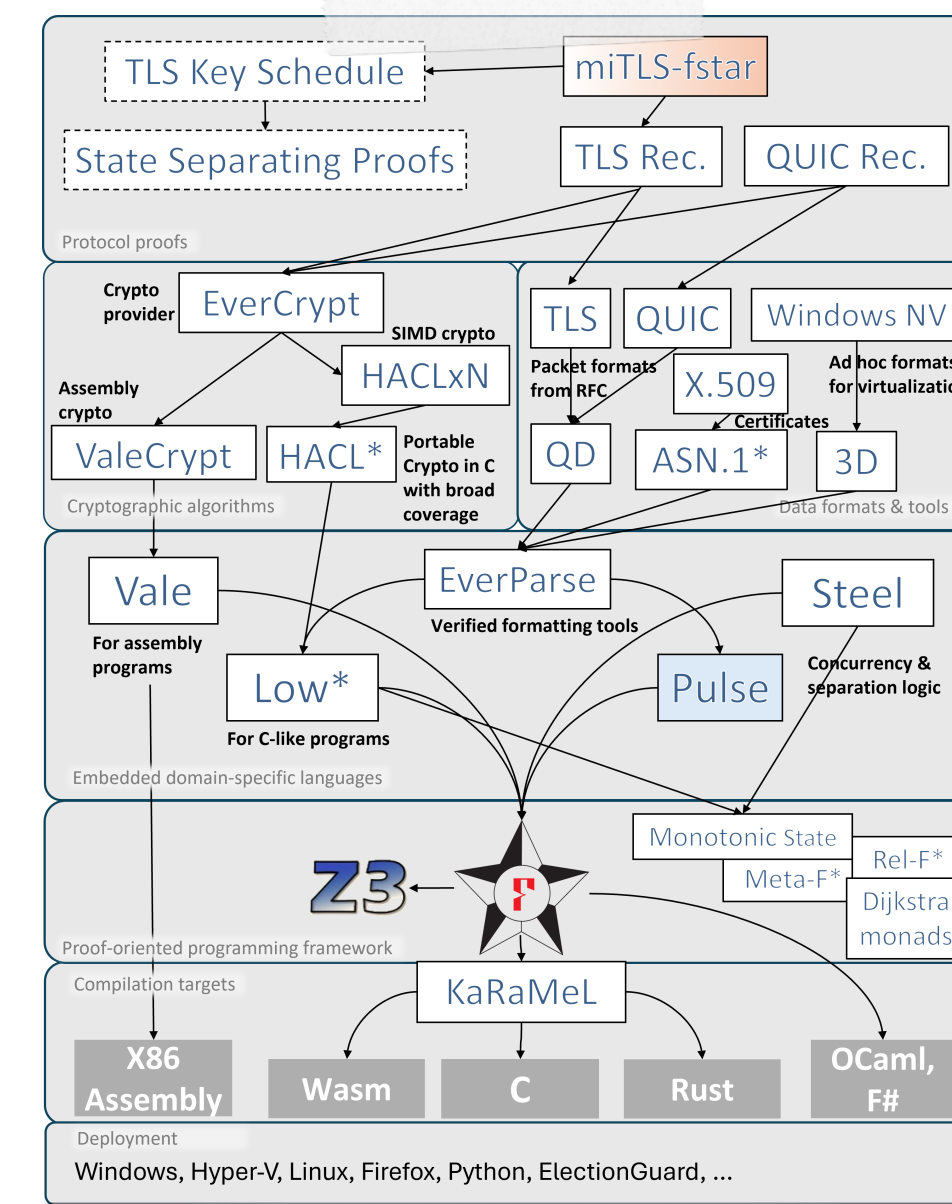
Programming Languages Lab, Peking University

Towards Safer Systems Software

formal verification to the rescue?



COMPCERT



Towards Safer Systems Software

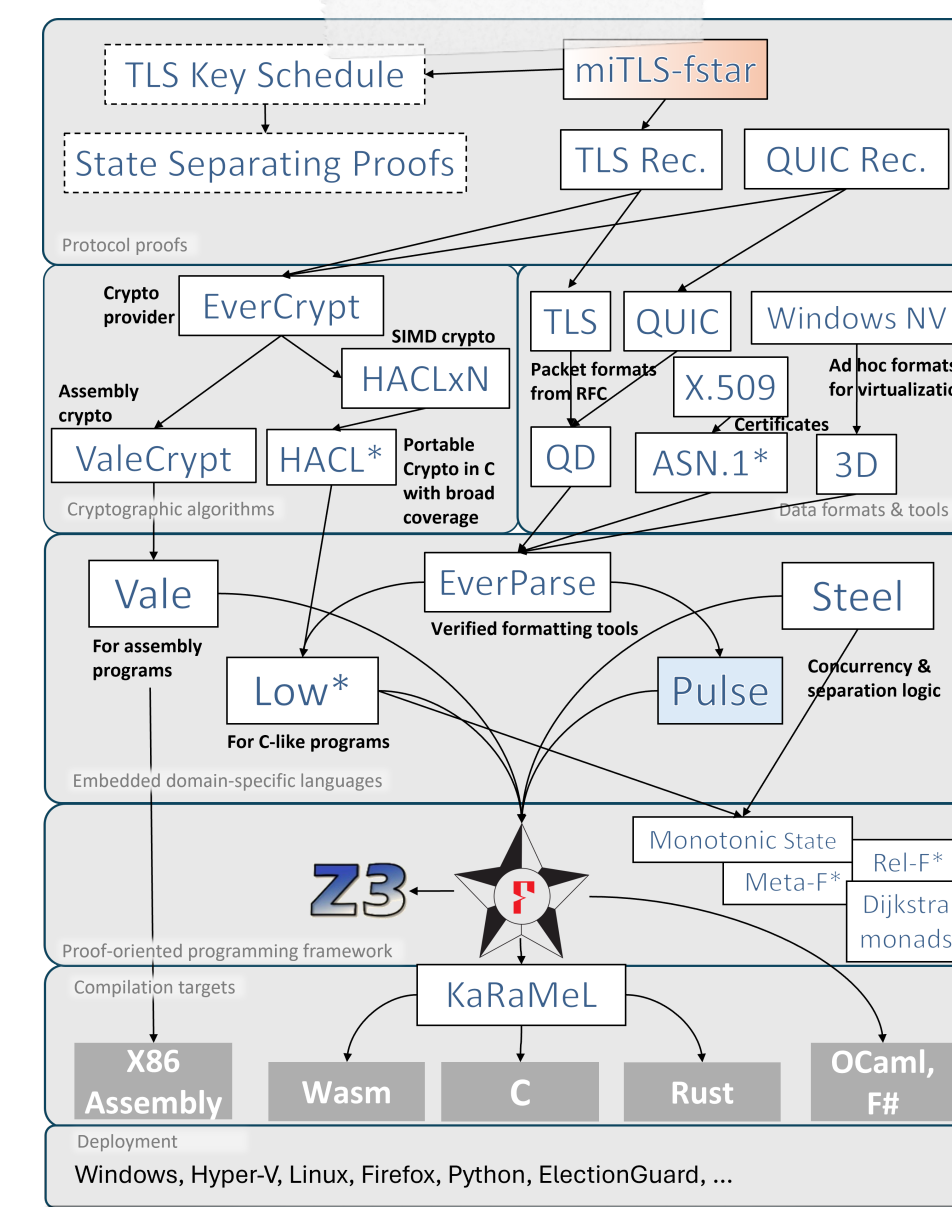
formal verification to the rescue?



verified kernels



COMPCERT



Towards Safer Systems Software

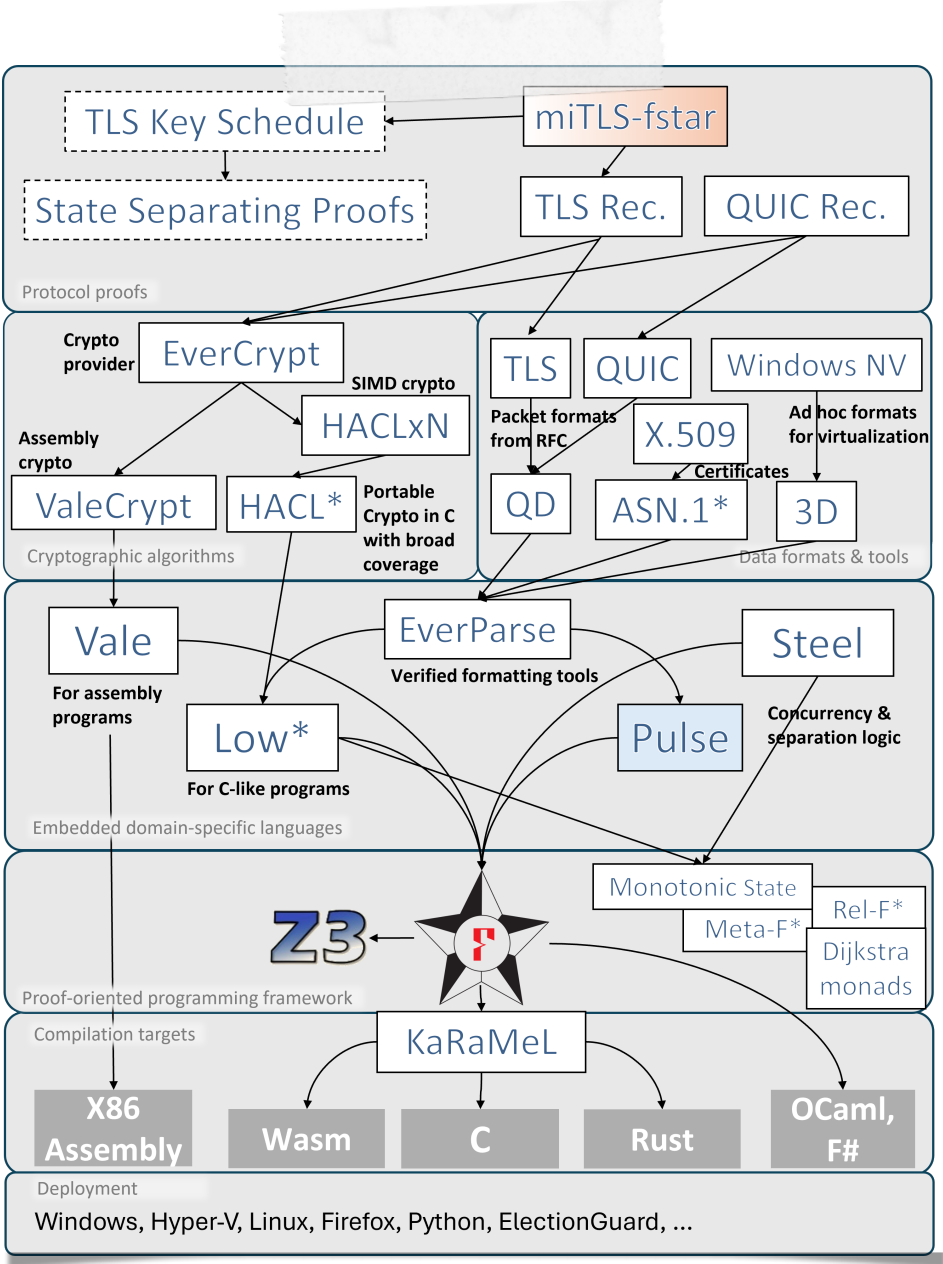
formal verification to the rescue?



verified kernels



verified compilers



Towards Safer Systems Software

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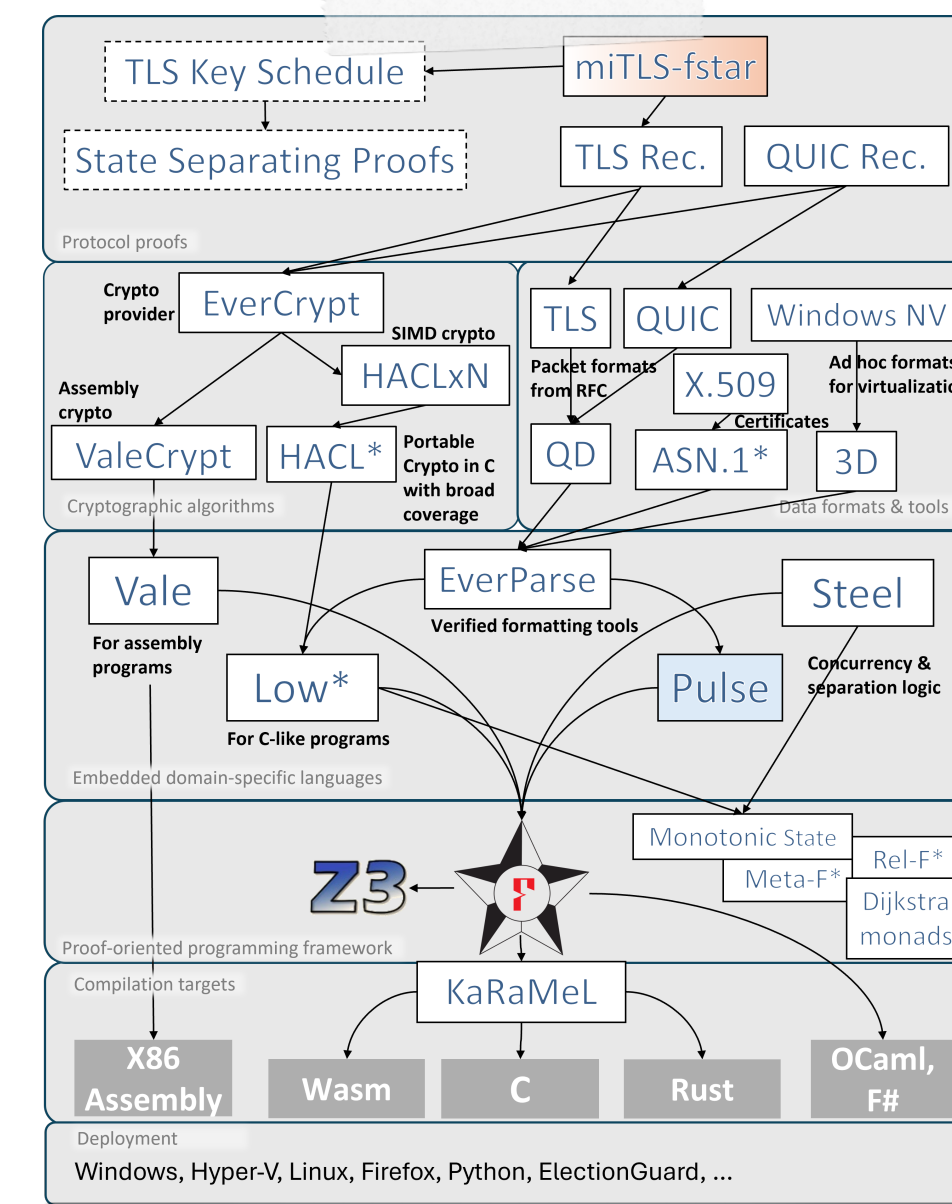


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verified compilers



verified protocols

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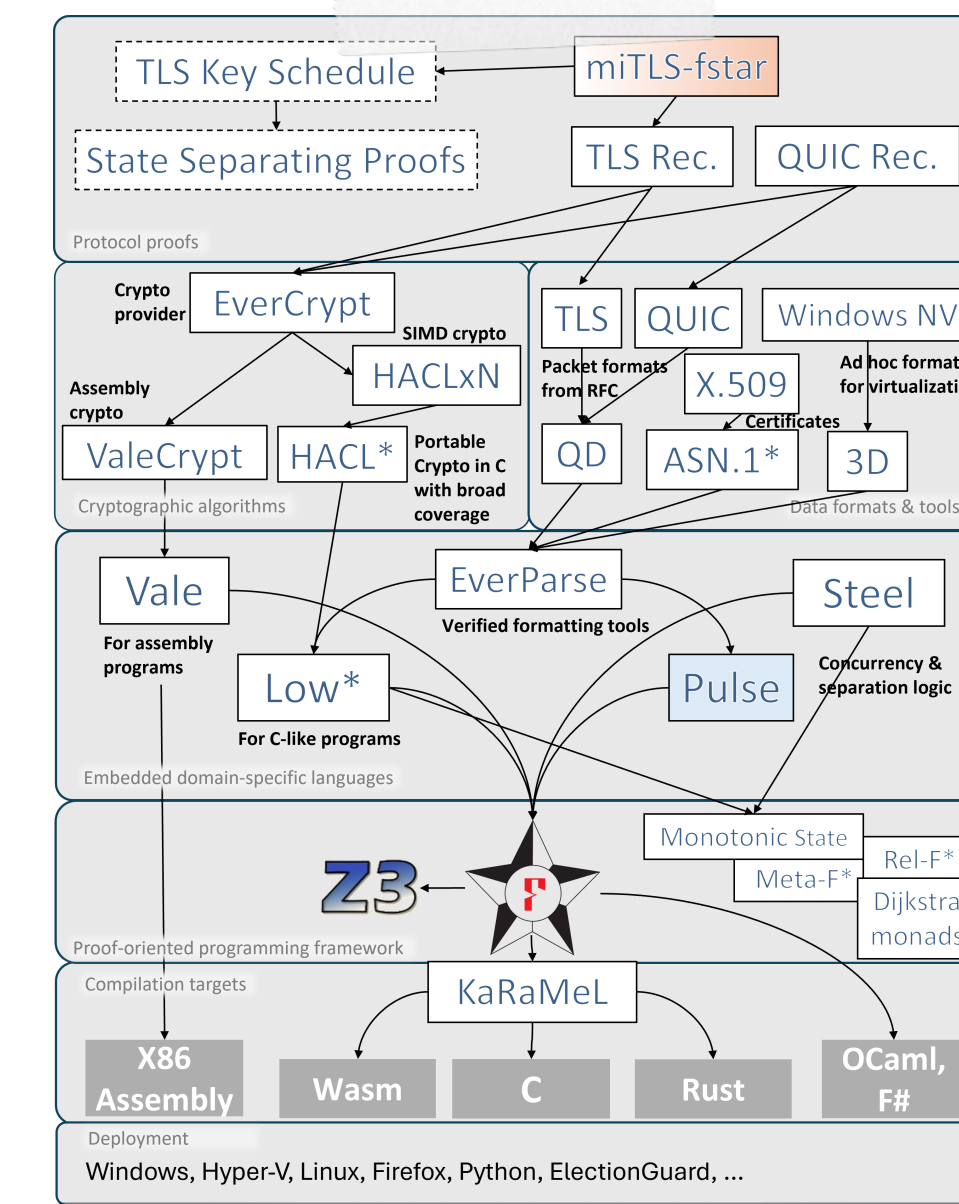
Isabelle/HOL
HOL4



verified kernels

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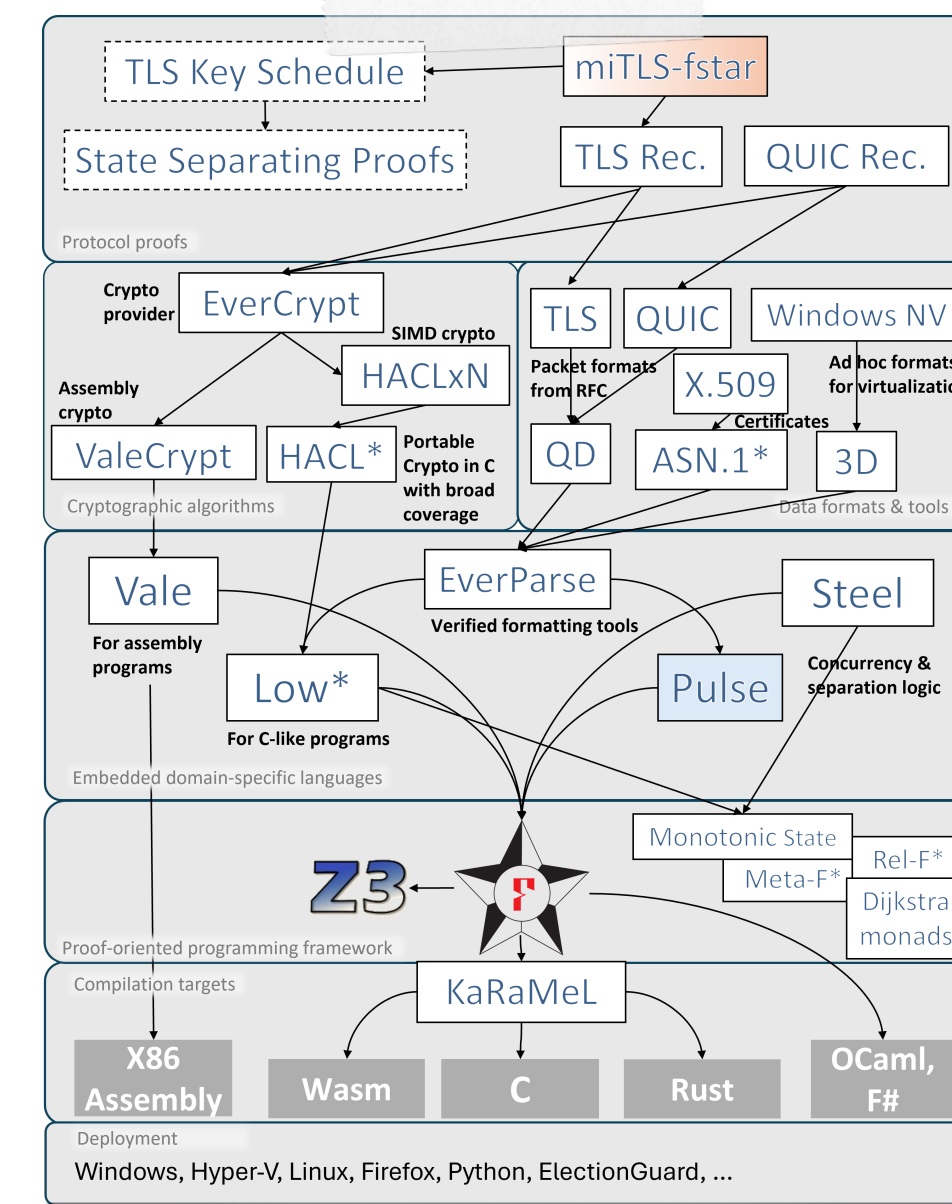
Rocq
(formerly Coq)



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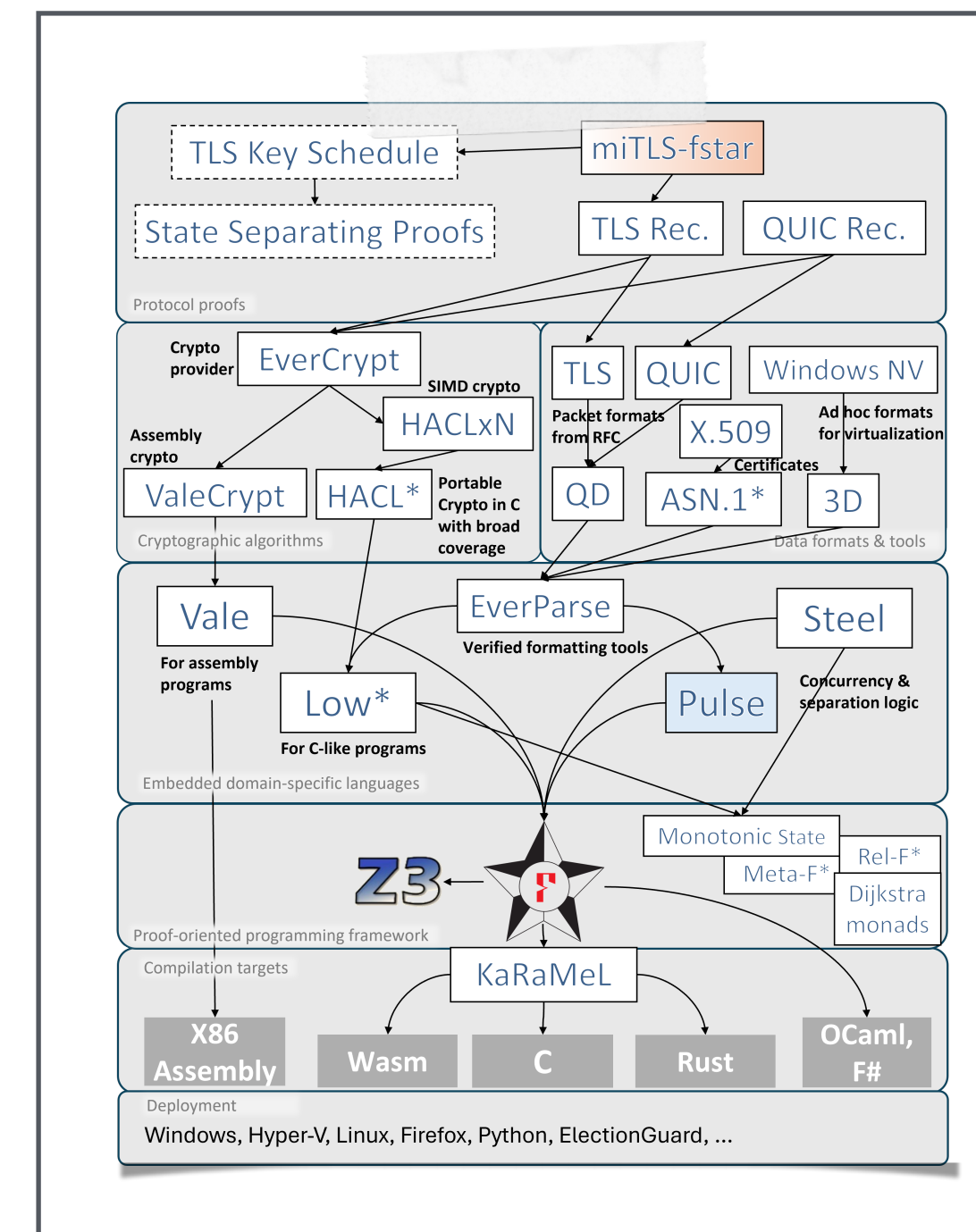
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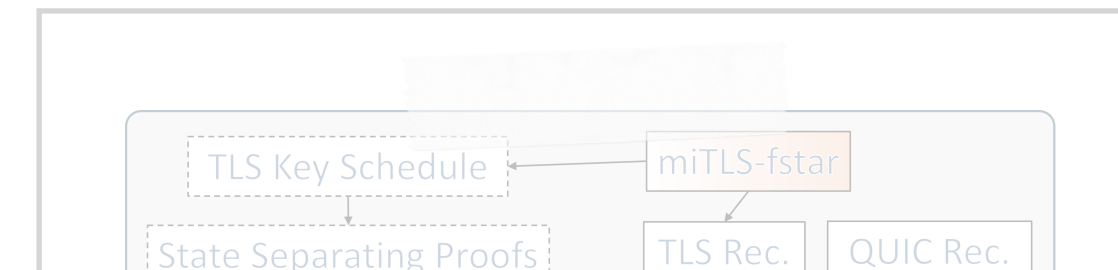
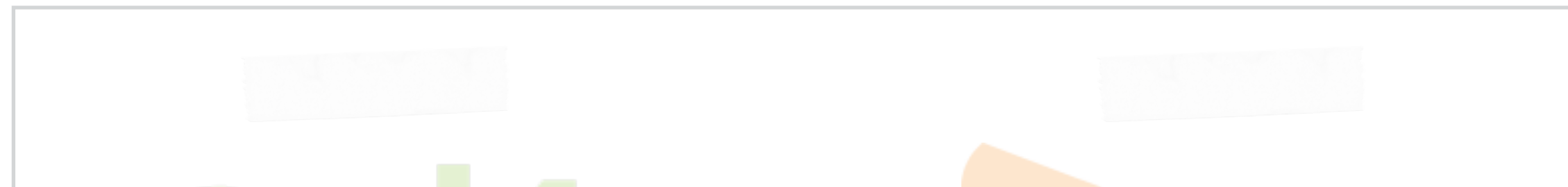
Dafny
F*

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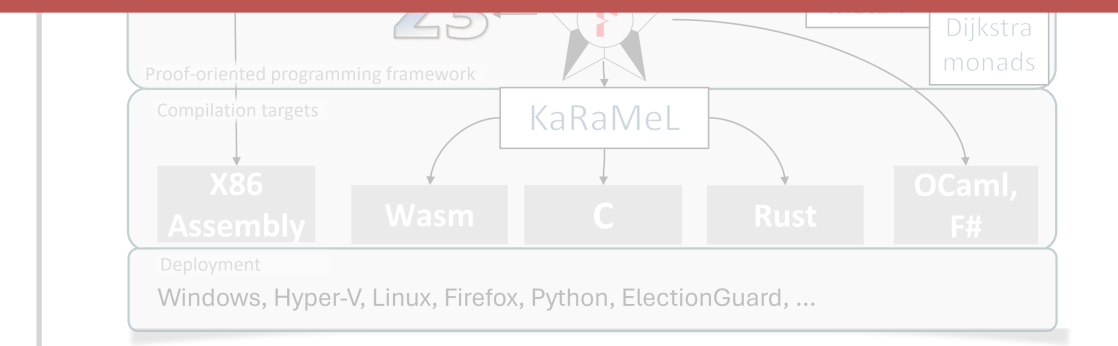
fny
*

"theorem prover" sounds scary

R
(formerly Coq)



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verified kernels

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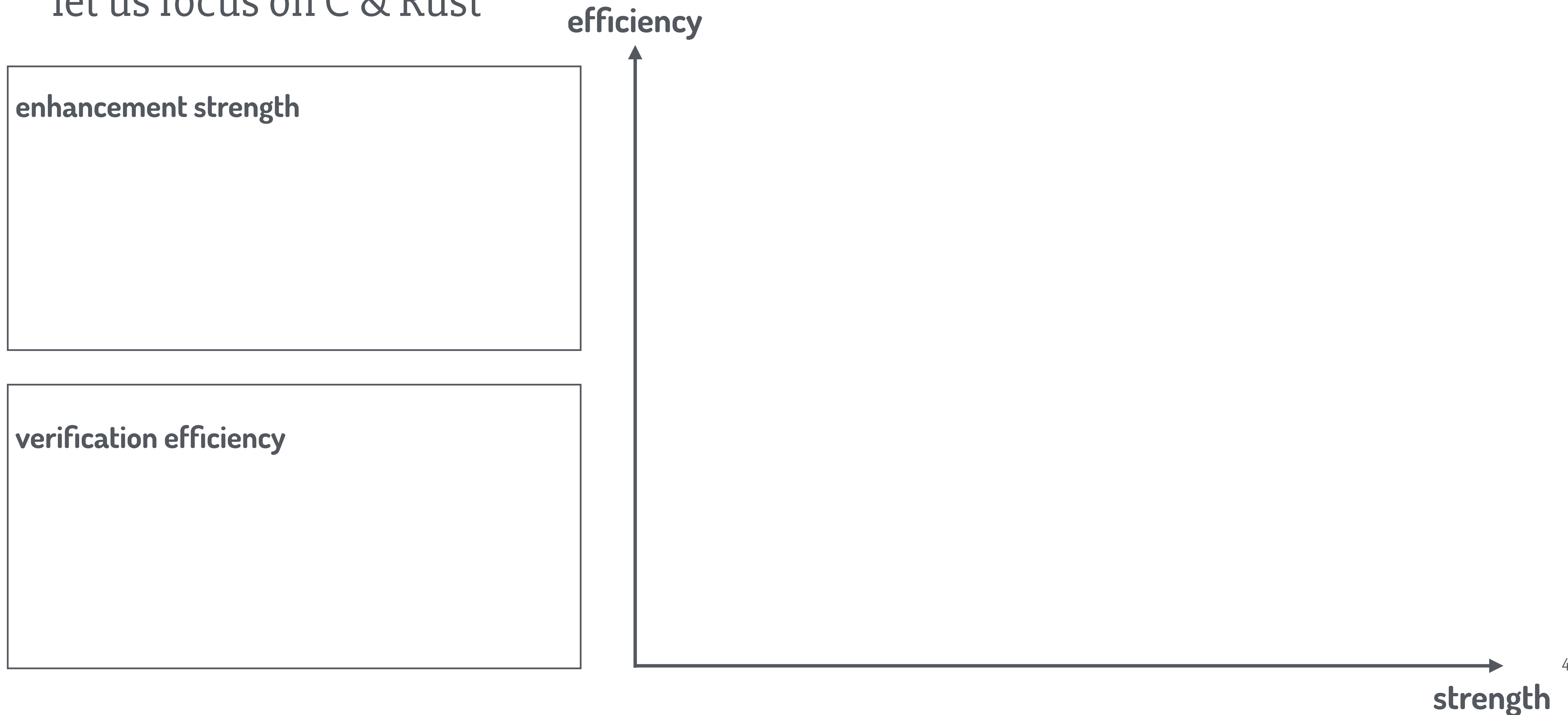
Language Enhancement?

let us focus on C & Rust



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Language Enhancement?

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enhancement strength

● verified properties: memory / thread safety, functional correctness, security, ...

verification efficiency

efficiency

strength

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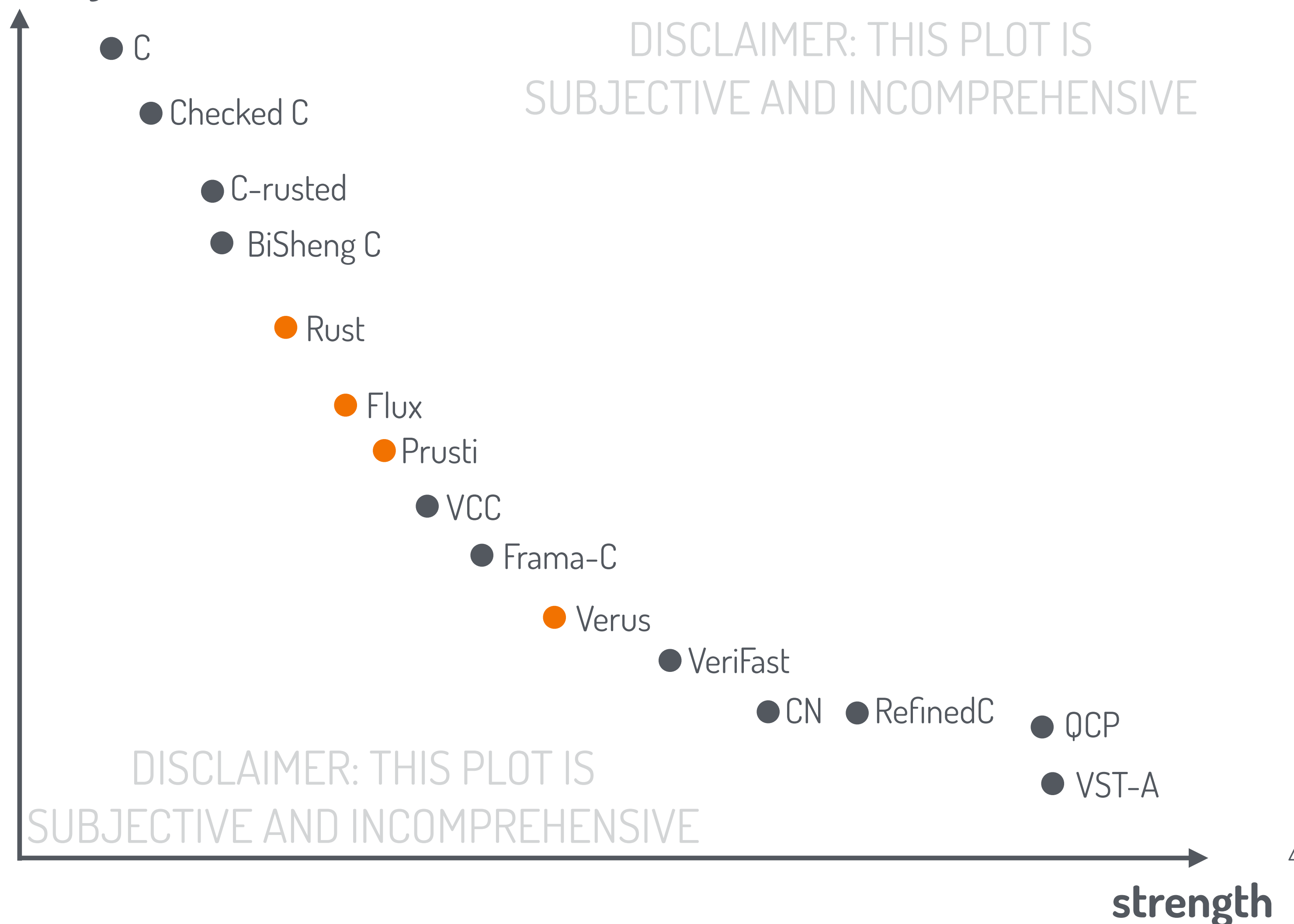
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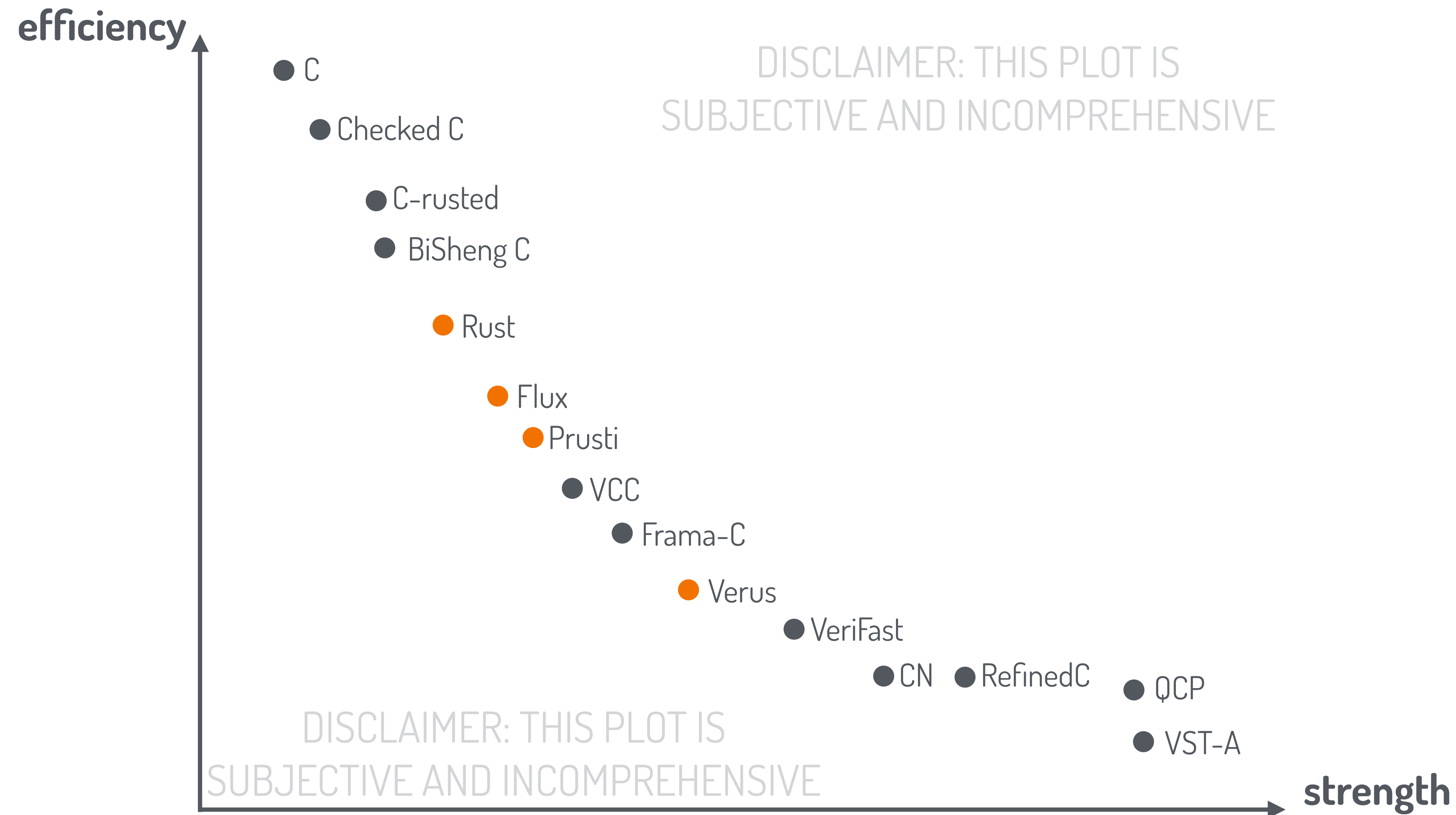
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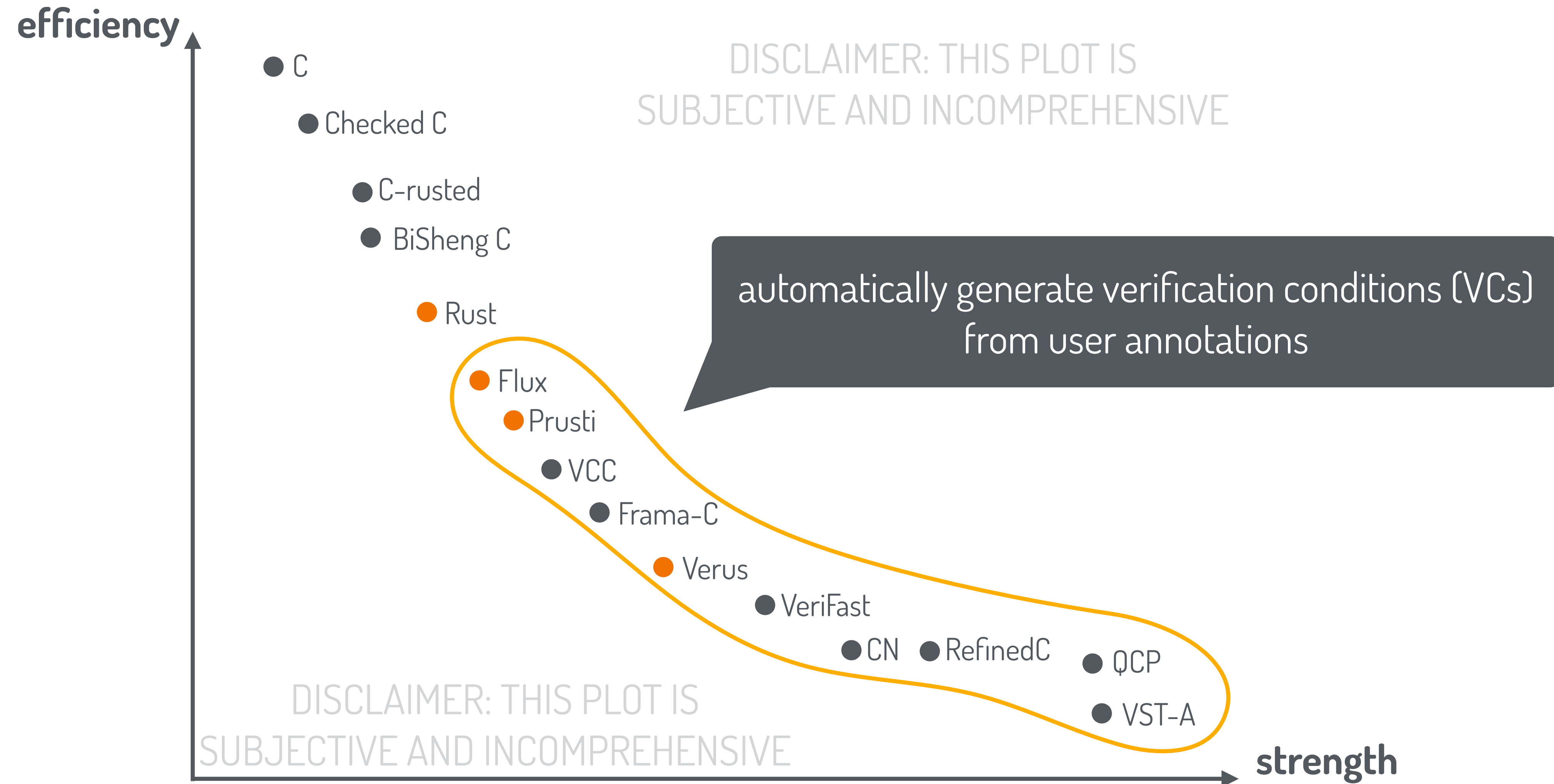
Obs I: VC Generation is Required

if aiming for high efficiency



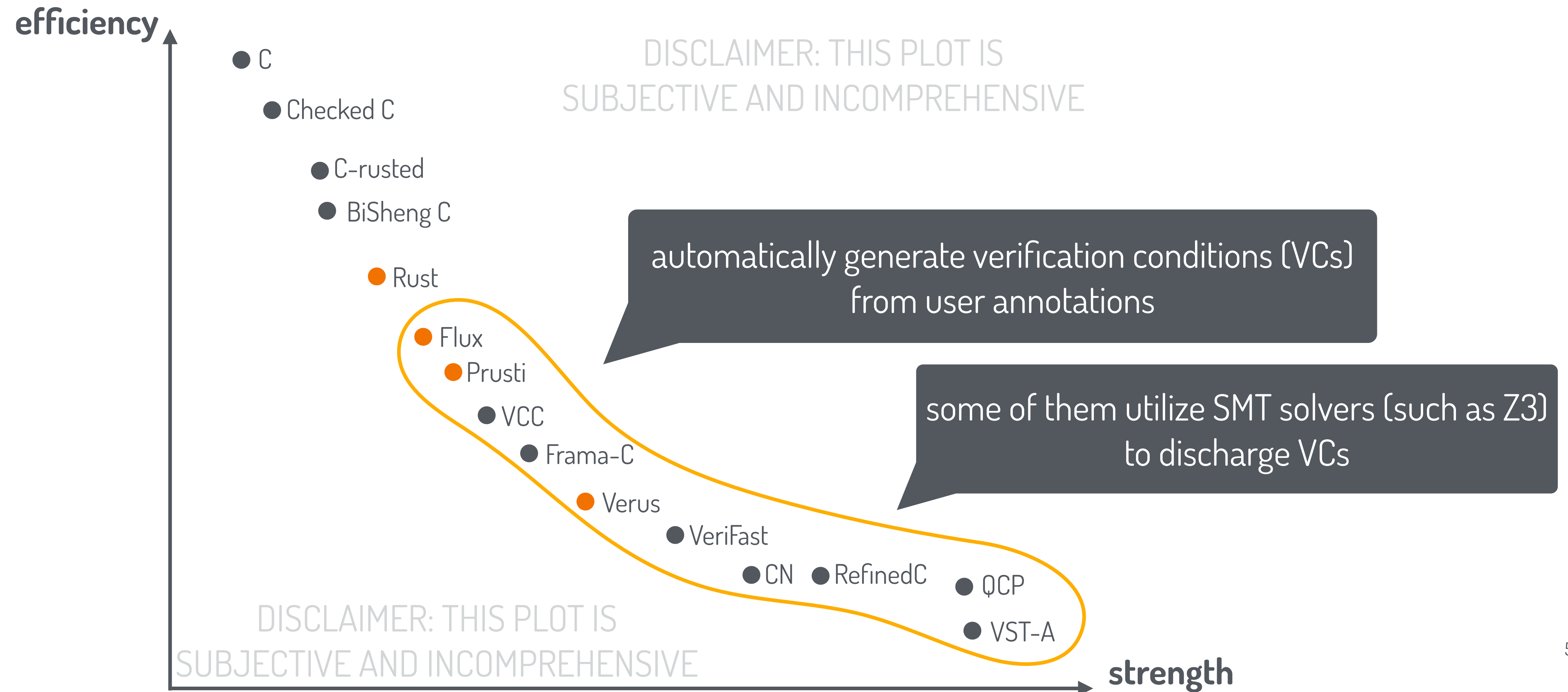
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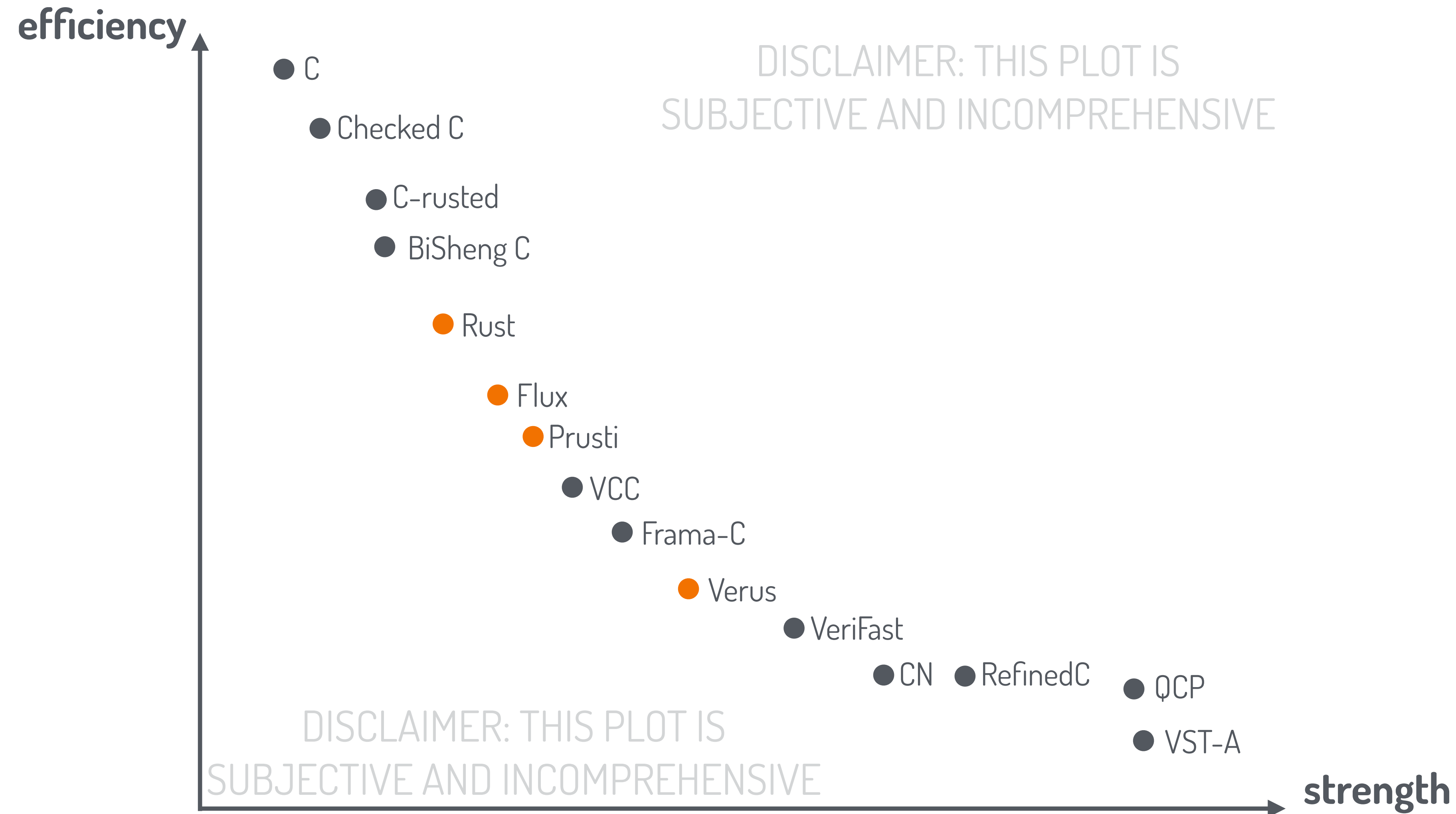


CStar Demo: VC Generation

nothing new yet

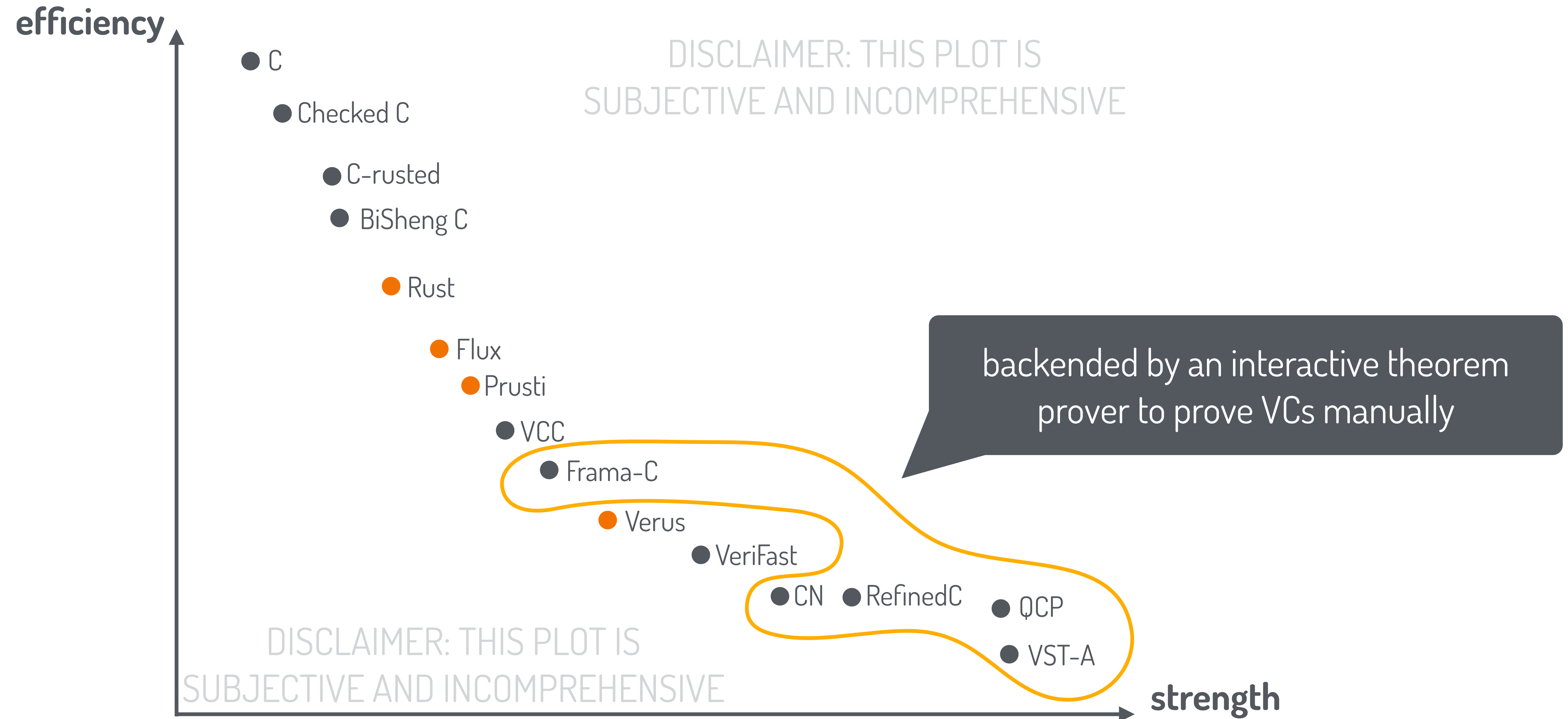
Obs: Manual Proof is Unavoidable

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Prob I: Proof Encapsulation

theorem provers are nice, but ...

current status in CN (and many others):
proofs are delegated to Rocq

```
lemma append_nil (datatype seq l1)
  requires true;
  ensures append(l1, Nil {}) == l1;

lemma append_cons (datatype seq l1, i32 x, datatype seq l2)
  requires true;
  ensures append(l1, Cons {head: x, tail: l2})
    == append(snoc(l1, x), l2);
```

```
struct node *tmp = cur->tail;
cur->tail = last;
last = cur;
cur = tmp;
/*@ unfold rev(L2); @*/
/*@ apply append_cons (rev (tl(L2)), hd(L2), L1); @*/
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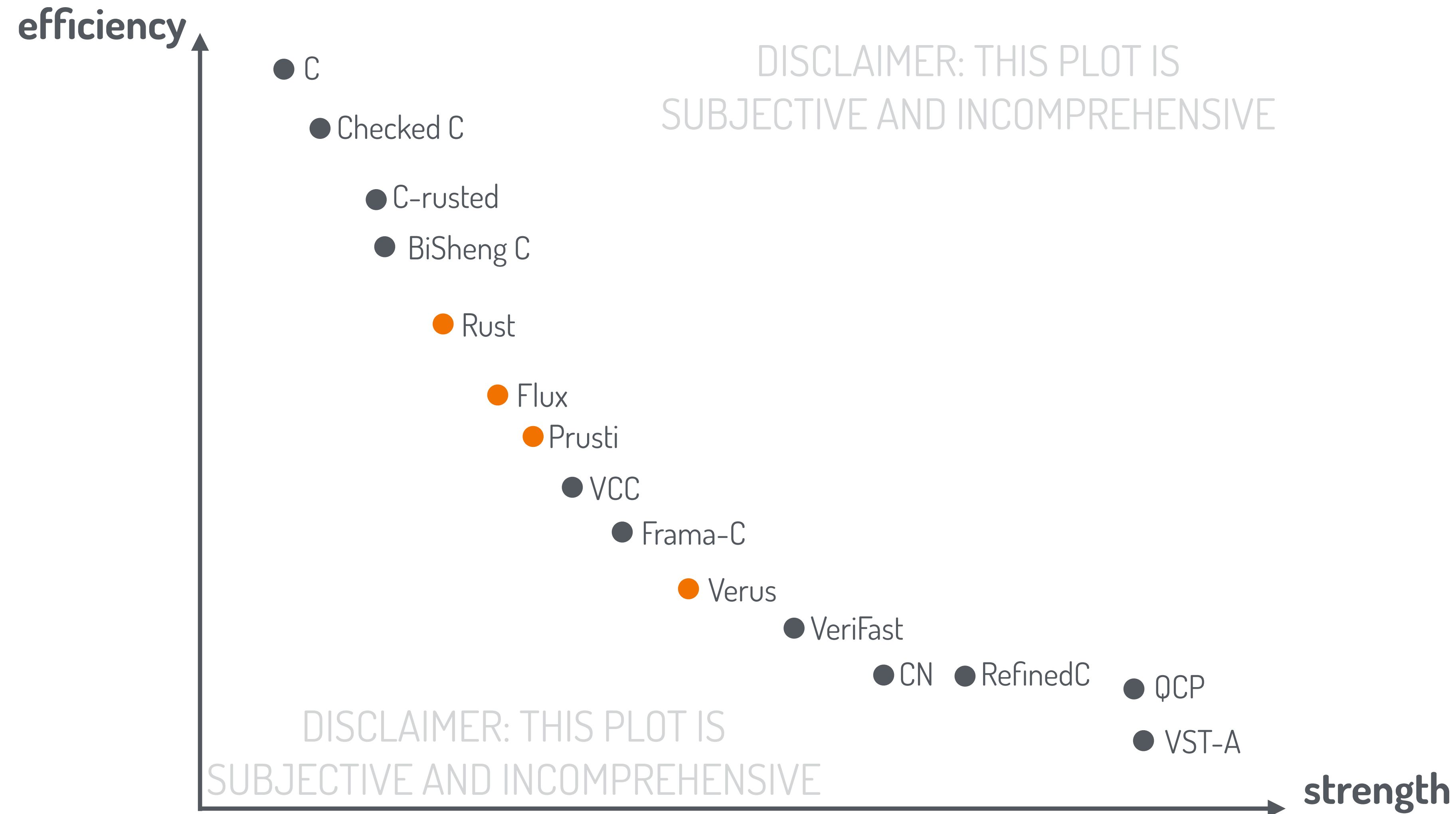
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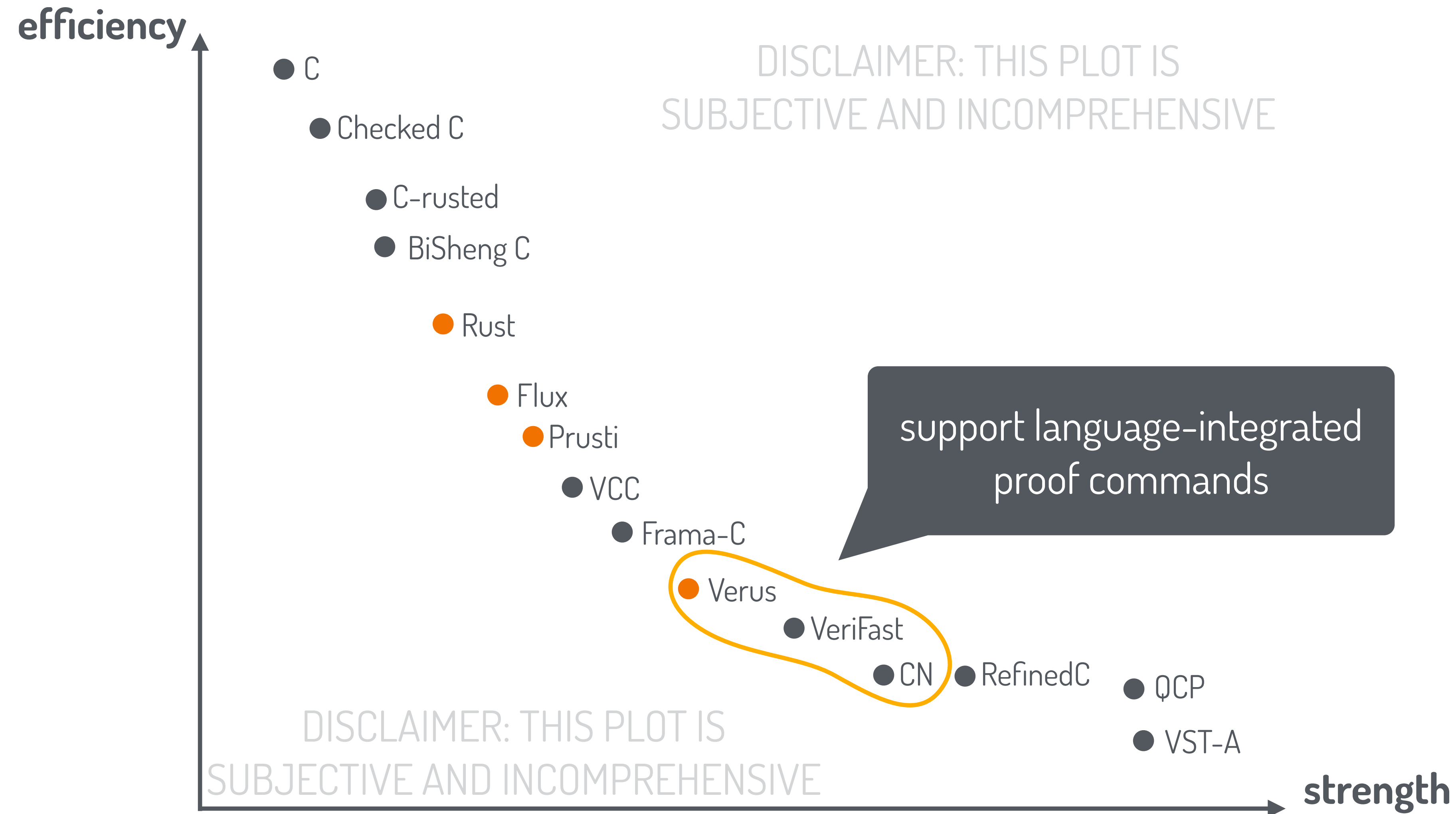
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```
struct node *reverse(struct node *xs)
/*@ requires take L = IntList(xs);
    ensures  take L_ = IntList(return);
            L_ == rev(L);

@*/
{

    struct node *last = 0;
    struct node *cur = xs;
    /*@ apply append_nil(rev(L)); @*/
    while(1)
    /*@ inv take L1 = IntList(last);
        take L2 = IntList(cur);
        append(rev(L2), L1) == rev(L);

    @*/
    {
        if (cur == 0) {
            /*@ unfold rev(Nil {}); @*/
            /*@ unfold append(Nil {}, L1); @*/

            return last;
        }
        struct node *tmp = cur->tail;
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```

example program with proof commands in CN


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    }
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```

example program with proof commands in CN

```

public boolean remove(Object o)
/*: requires " init "
    modifies content, csize
    ensures
    "( result → (∃ i. (i,o)∈old content ∧
        (¬∃ j. j<i ∧ (j,o)∈old content) ∧
        (∀ j e. 0≤j∧j<i→(j,e)∈content=(j,e)∈old content) ∧
        (i≤j∧j<csize→(j,e)∈content=(j+1,e)∈old content)) ∧
        (¬result → (content=old content∧¬∃i. (i,o)∈old content)))" */
{
    int index = 0;
    while /*: inv "(∀j. 0≤j∧j<index→o≠elements.[j]) ∧
        0≤index ∧ size=old size" */
        (index < size) {
        if (elements[index] == o) {
            shift (index);
            /*: note ObjectRemoved:
                "∀j e. (0≤j∧j<index→(j,e)∈content=(j,e)∈old content) ∧
                (index≤j∧j<csize→(j,e)∈content=(j+1,e)∈old content)"
                from shift_Postcondition , LoopInv, LoopCondition
                    content_def, csize_def;

                witness index for
                "∃i. (i,o)∈old content ∧ (¬∃j. j<i ∧ (j,o)∈old content) ∧
                (∀j e. (0≤j∧j<i→(j,e)∈content=(j,e)∈old content) ∧
                (i≤j∧j<csize→(j,e)∈content=(j+1,e)∈old content)))" */
            return true;
        }
        index = index + 1;
    }
    return false ;
}

```

example program with proof commands in Jahob

Prob II: Programmable Proof

proof commands are nice, but ...

```

p ::= p1 ; p2
      | assert l: F from  $\vec{h}$ 
      | note l:F from  $\vec{h}$ 
      | localize in (p ; note l:F)
      | mp l:(F → G)
      | assuming lF:F in (p ; note lG:G)
      | cases  $\vec{F}$  for l:G
      | showedCase i of l : F1 ∨ ... ∨ Fn
      | byContradiction l:F in p
      | contradiction l:F
      | instantiate l:∀ $\vec{x}$ .F with  $\vec{t}$ 
      | witness  $\vec{t}$  for l:∃ $\vec{x}$ .F
      | pickWitness  $\vec{x}$  for lF:F in (p ; note lG:G)
      | pickAny  $\vec{x}$  in (p ; note l:F)
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```

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- obs: manual proofs are inevitable for complex reasoning tasks

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```

Prob II: Programmable Proof

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- obs: using a fixed set of proof commands feels neither comprehensive nor extensible

principle: support using the full language to **programmatically** construct proof

```

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    | assert l : F from  $\vec{h}$ 
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    | localize in (p ; note l : F)
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The LCF Solution

logic for computable functions





The LCF Solution

logic for computable functions

© the **LCF architecture** for theorem proving by Robin Milner in the 1970s

The LCF Solution

logic for computable functions

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- © programming formal proof is to **compute theorems** using a **protected interface**

IMPLEMENTED IN A SINGLE PROGRAMMING LANGUAGE WITH TYPE ABSTRACTION



The LCF Solution

logic for computable functions

- ◎ the **LCF architecture** for theorem proving by Robin Milner in the 1970s
- ◎ programming formal proof is to **compute theorems** using a **protected interface**
- ◎ **correct-by-construction** even when extended with arbitrary user proof code

IMPLEMENTED IN A SINGLE PROGRAMMING LANGUAGE WITH TYPE ABSTRACTION





CStar Demo: Proof Programming

a practice of LCF in C





it is now already possible to prove VCs in C

it is now already possible to prove VCs in C

but we can do better by introducing
program-proof states

CStar Demo: Program-Proof State

essentially, a **symbolic** representation of the program state



a VC is a prop "**pre** |-- **post**" at a program point

both are program-proof states

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proving a VC is **coupled** with programming in CStar

both are program-proof states

a VC is a prop "**pre** |-- **post**" at a program point

proving a VC is **coupled** with programming in CStar
you write a proof to transform from **pre** to **post**



CStar Demo: Program Proof

unify program and proof

The Architecture of CStar

how to ensure correct-by-construction





The Architecture of CStar

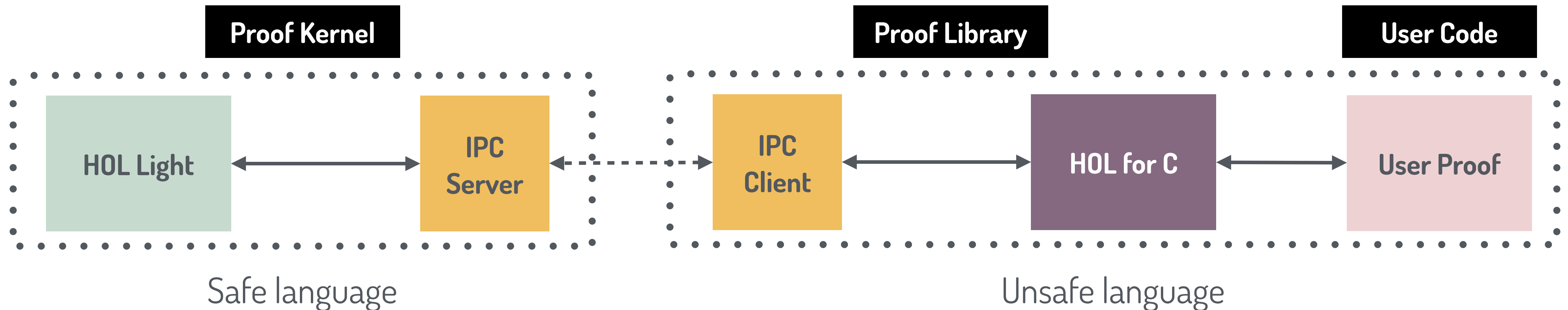
how to ensure correct-by-construction

- © the original LCF design heavily relies on **type abstraction** provided by the ML language

The Architecture of CStar

how to ensure correct-by-construction

- the original LCF design heavily relies on **type abstraction** provided by the ML language
- we worked out a **language-agnostic** variant of the LCF-architecture with **process separation**





The Architecture of CStar

how to maintain the program-proof states



The Architecture of CStar

how to maintain the program-proof states

◎ compute symbolic heap information via **forward symbolic execution**



The Architecture of CStar

how to maintain the program-proof states

- compute symbolic heap information via **forward symbolic execution**
- CStar now employs (but is largely **agnostic** of) QCP's symbolic executor for **separation-logic** reasoning

QCP: A Practical Separation Logic-based C Program Verification Tool

Xiwei Wu¹, Yueyang Feng^{1,*}, Xiaoyang Lu^{1,*}, Tianchuan Lin¹, Kan Liu¹,
Zhiyi Wang², Shushu Wu¹, Lihan Xie¹, Chengxi Yang¹, Hongyi Zhong¹, Naijun
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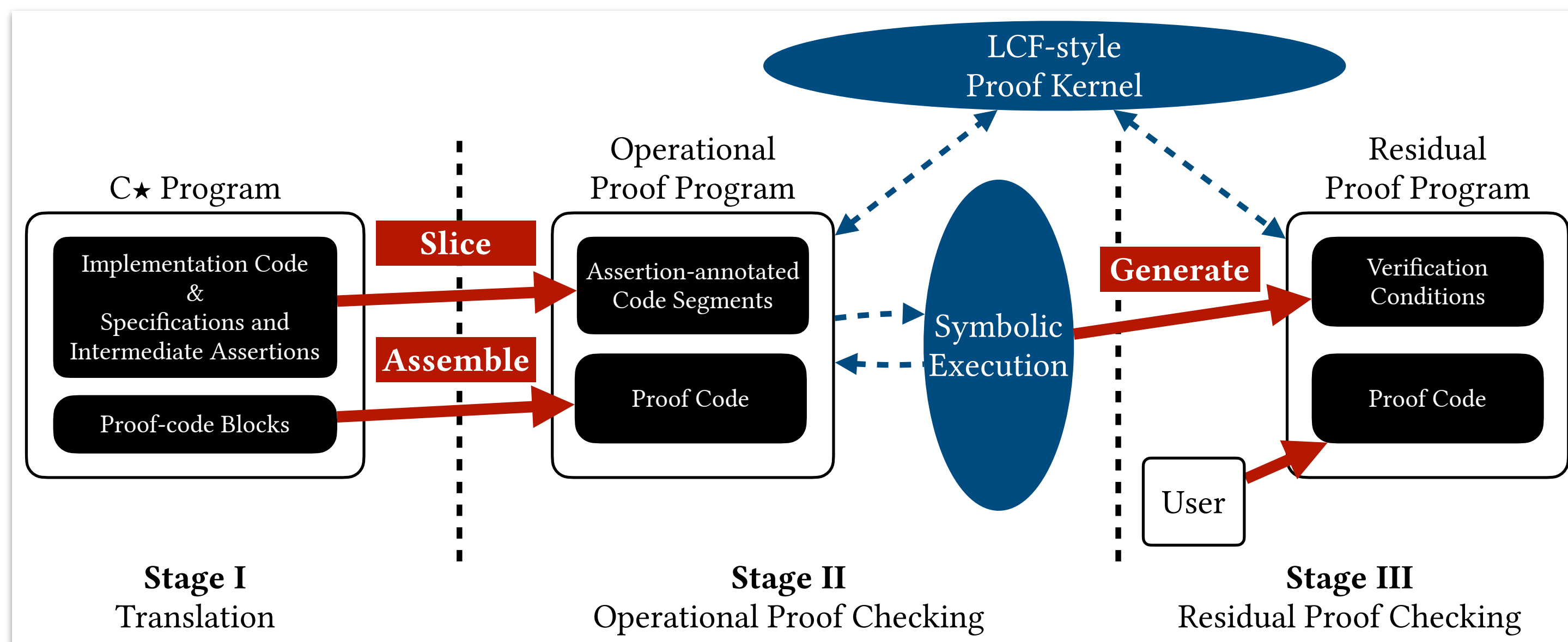
¹ Shanghai Jiao Tong University
{yashen, fyyvexoben, luxy1115, caoqinxiang}@sjtu.edu.cn

² Peking University
2301111964@stu.pku.edu.cn

The Architecture of CStar

how to maintain the program-proof states

- compute symbolic heap information via **forward symbolic execution**
- CStar now employs (but is largely **agnostic** of) QCP's symbolic executor for **separation-logic** reasoning
- QCP evolves the program-proof states for program code; CStar evolves the program-proof states for proof code



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² Peking University
2301111964@stu.pku.edu.cn

<https://arxiv.org/pdf/2505.12878>



users can now use **the full power of C**
to conduct proof and verification

CStar Demo: Tactics

all implemented outside the proof kernel



CStar Demo: SMT Integration

achieve controllable automation



CStar Demo: Proof Encapsulation

one can implement program-proof libraries

CStar

Unifying Programming and Verification in C





CStar

Unifying Programming and Verification in C

prob i: proof encapsulation

CStar

Unifying Programming and Verification in C

prob i: proof encapsulation

prob ii: programmable proof

CStar

Unifying Programming and Verification in C

prob i: proof encapsulation

prob ii: programmable proof

principle i: integrate **proof-specification-implementation** together into one language

CStar

Unifying Programming and Verification in C

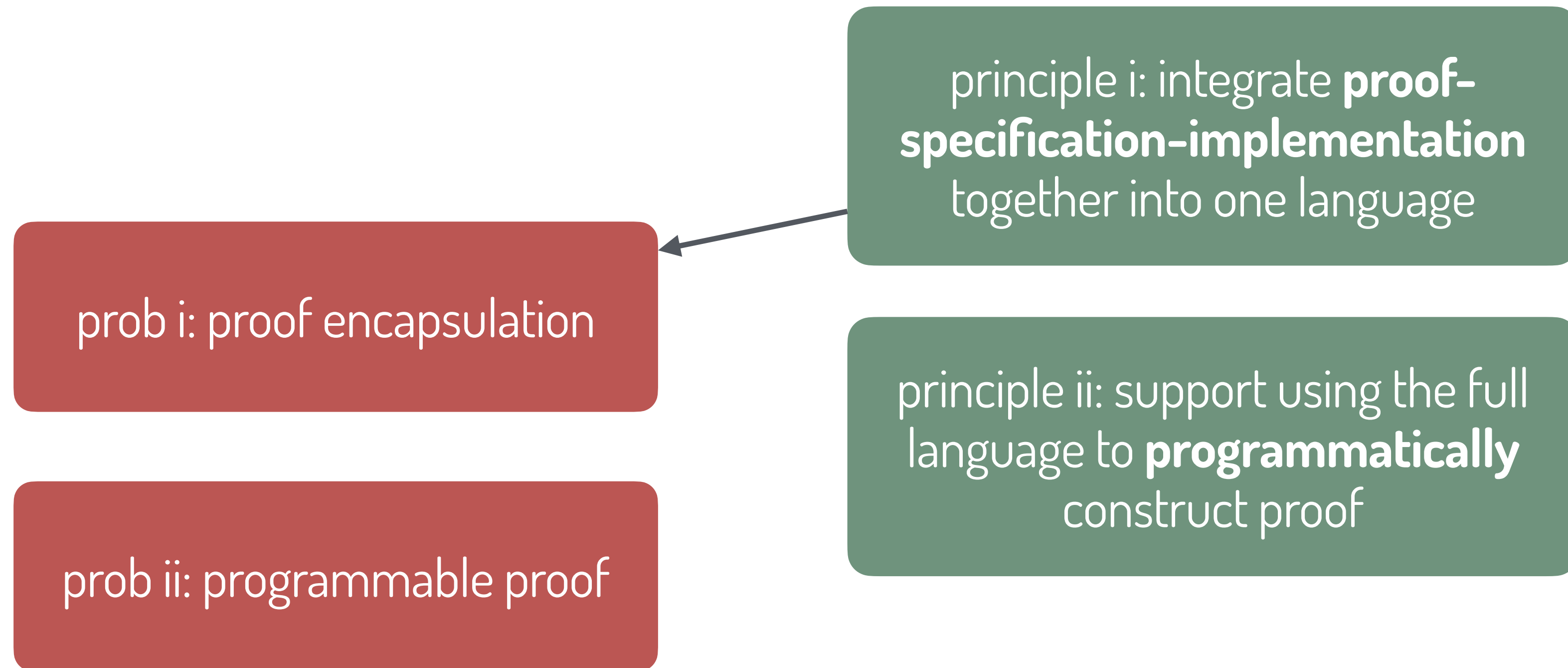
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prob i: proof encapsulation

prob ii: programmable proof

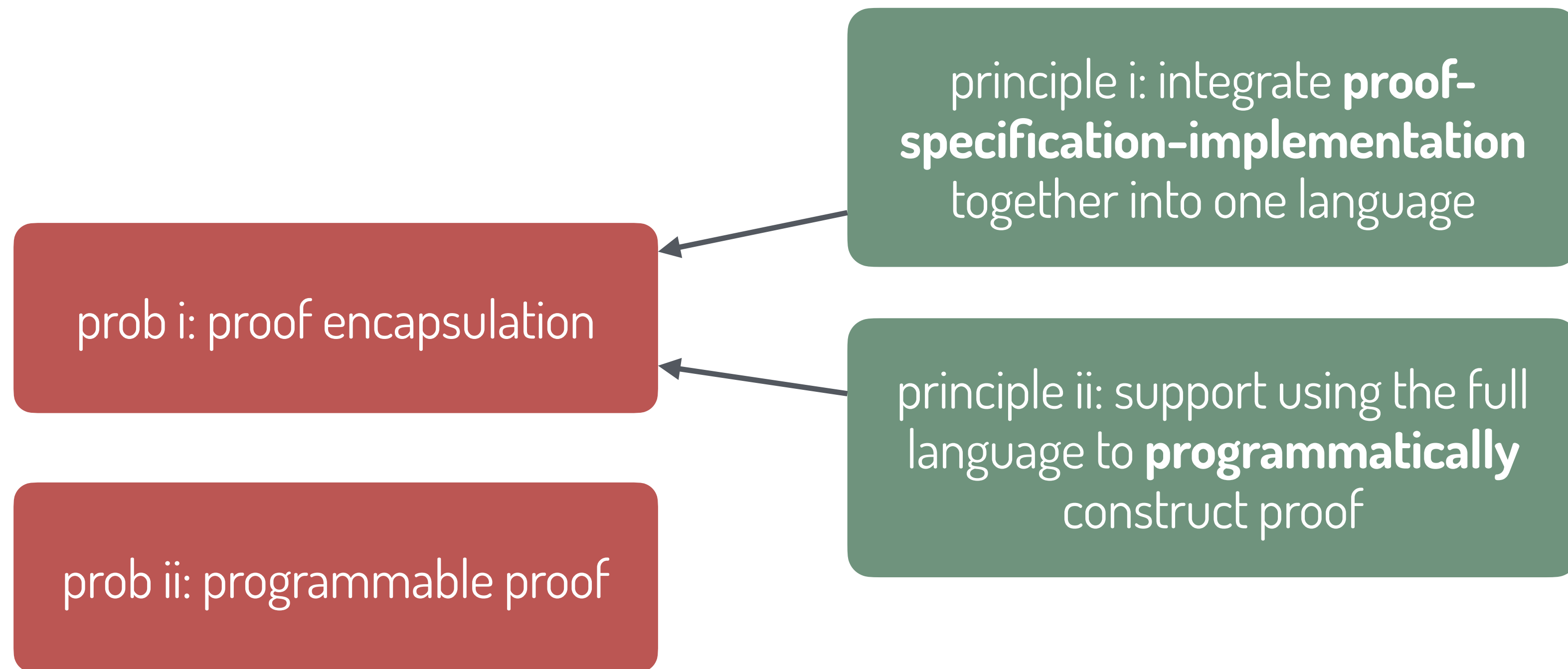
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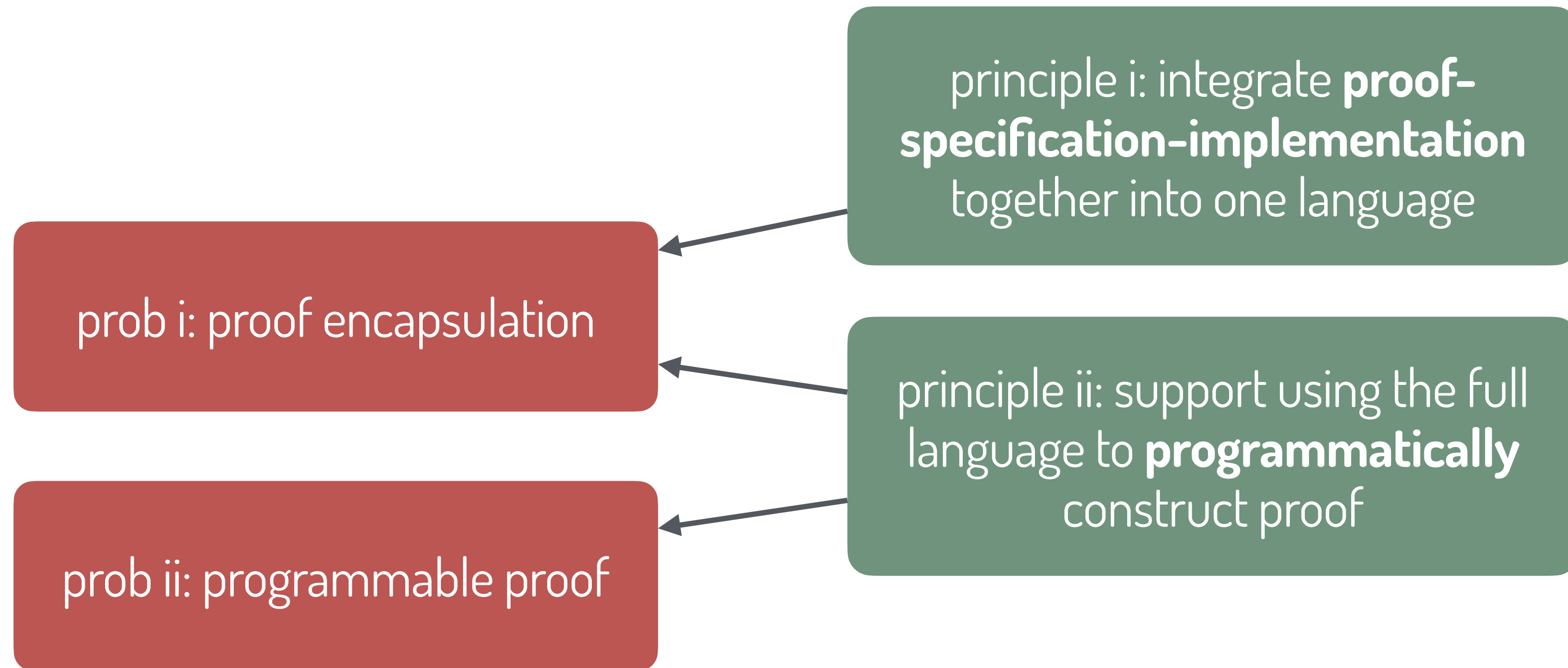
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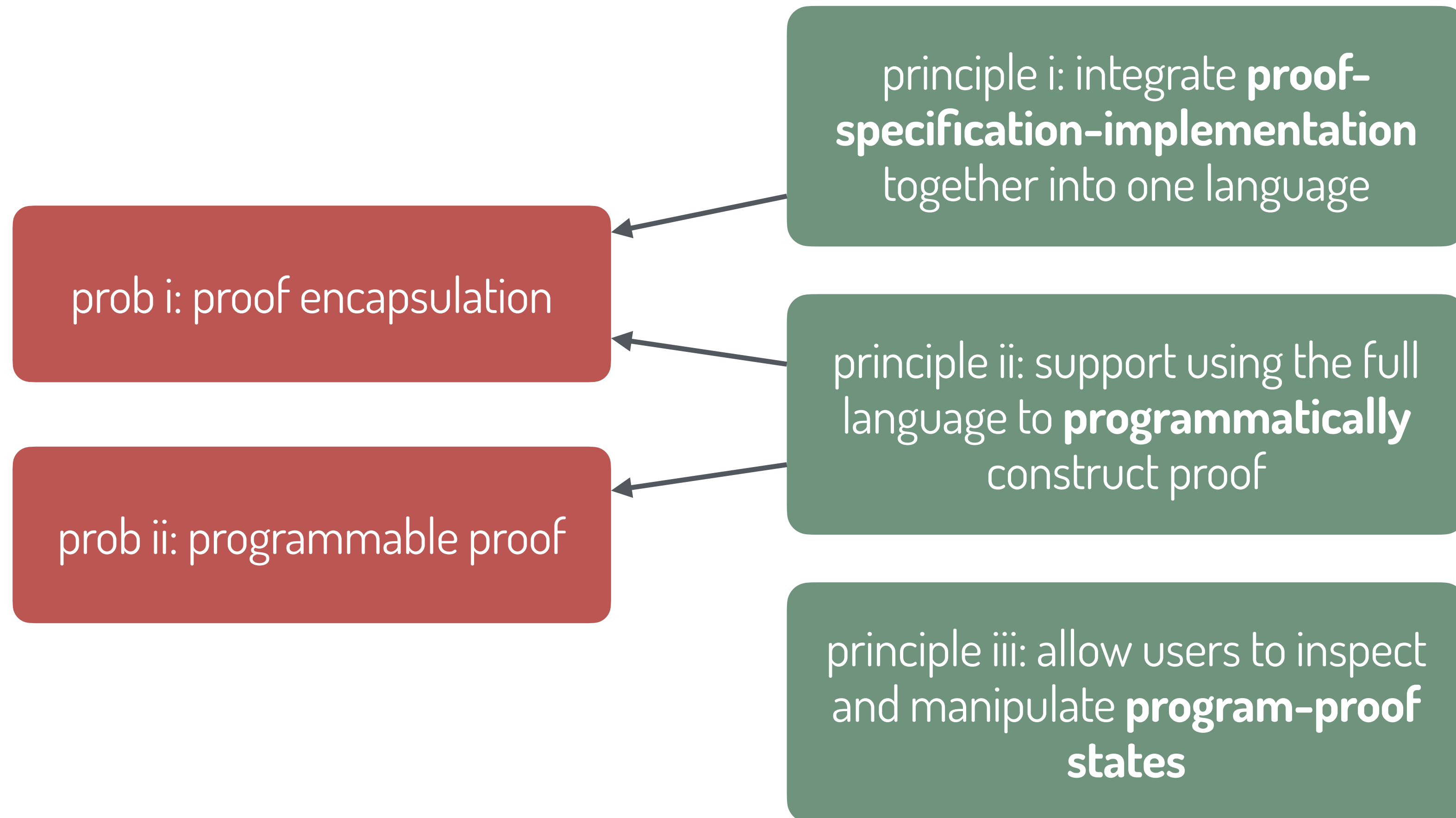
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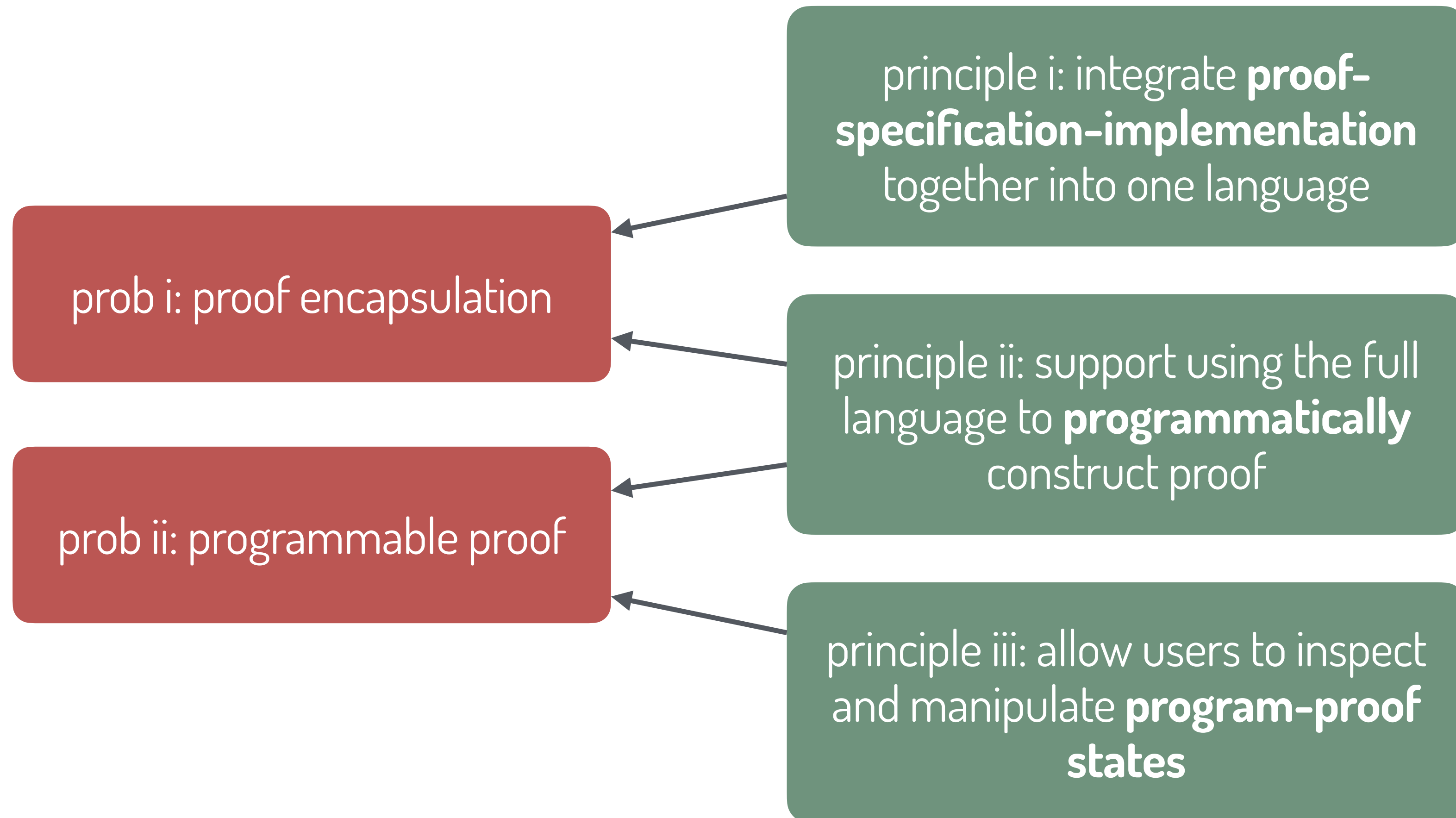
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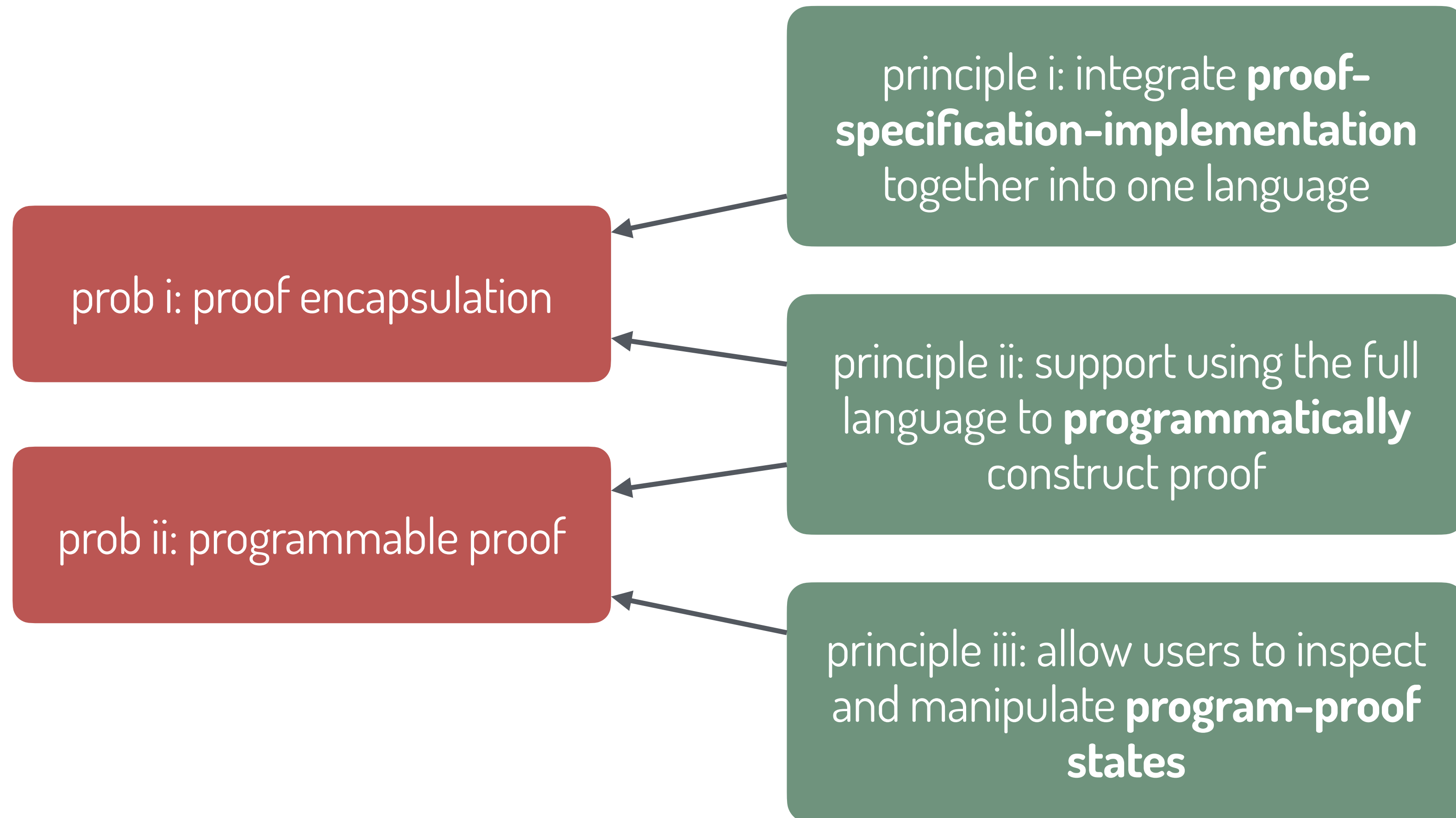
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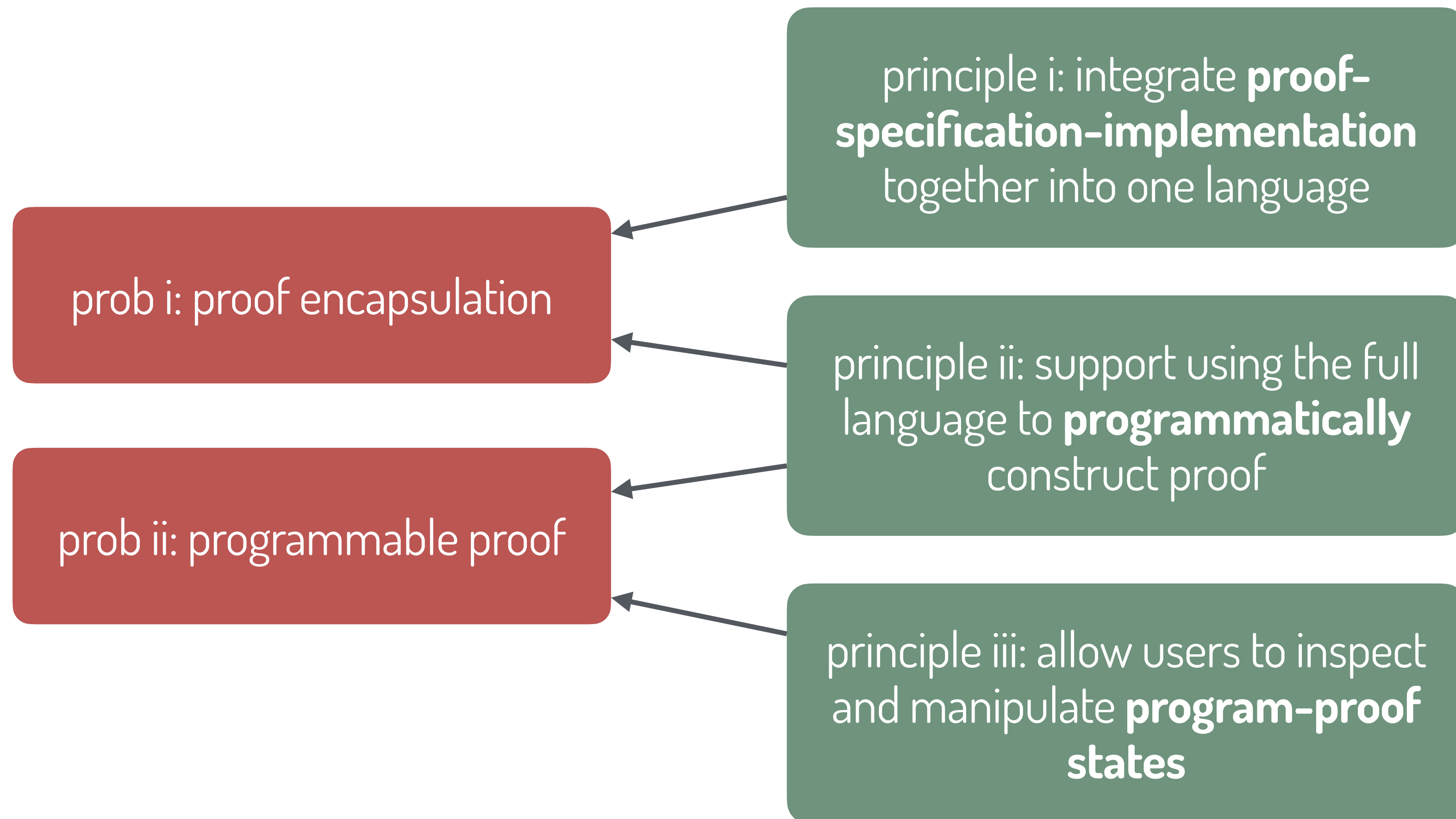
Unifying Programming and Verification in C



- ◎ **CStar reuses clang's toolchain**
 - ◎ use clang for compilation
 - ◎ use clangd for language server

CStar

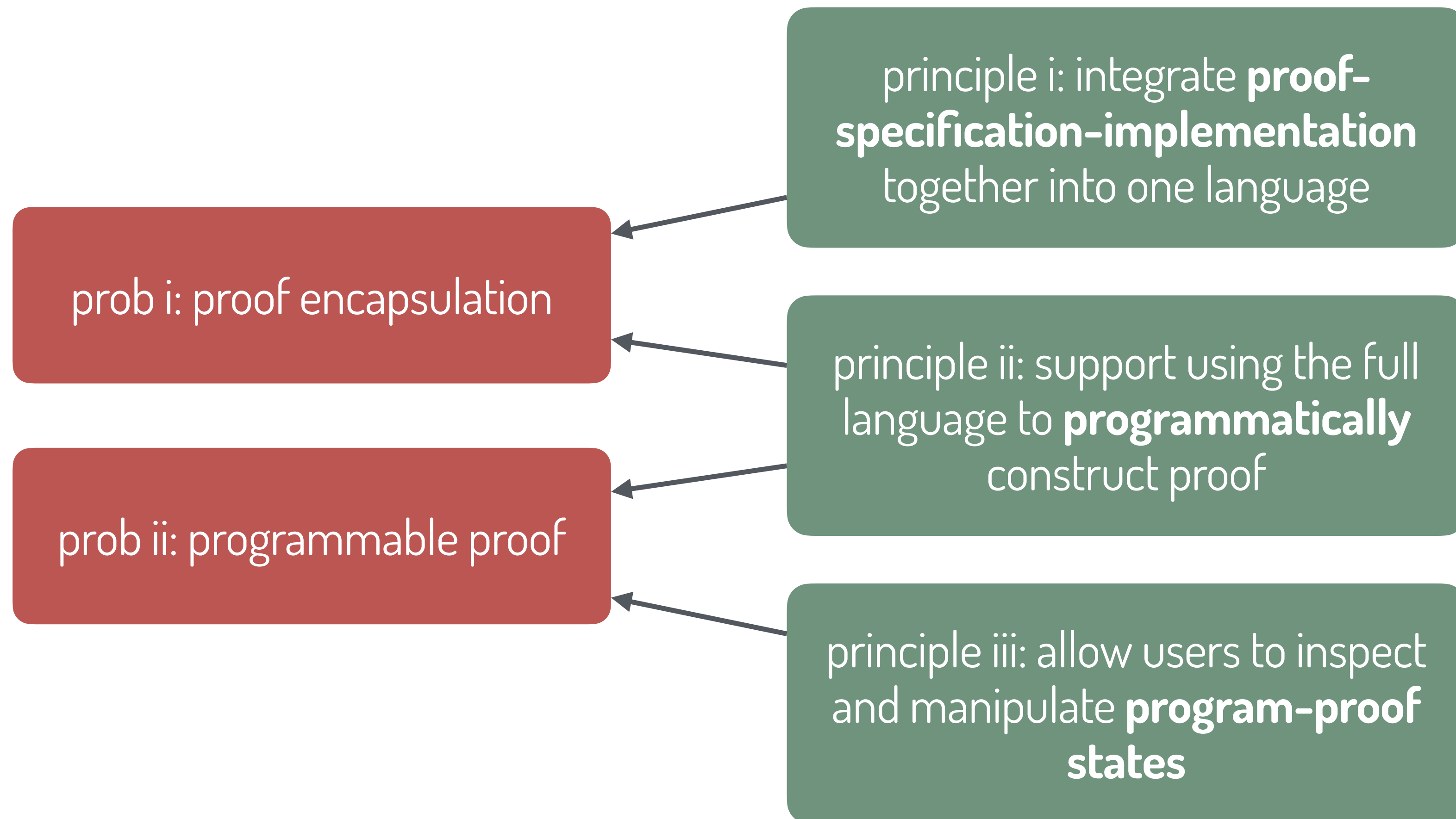
Unifying Programming and Verification in C



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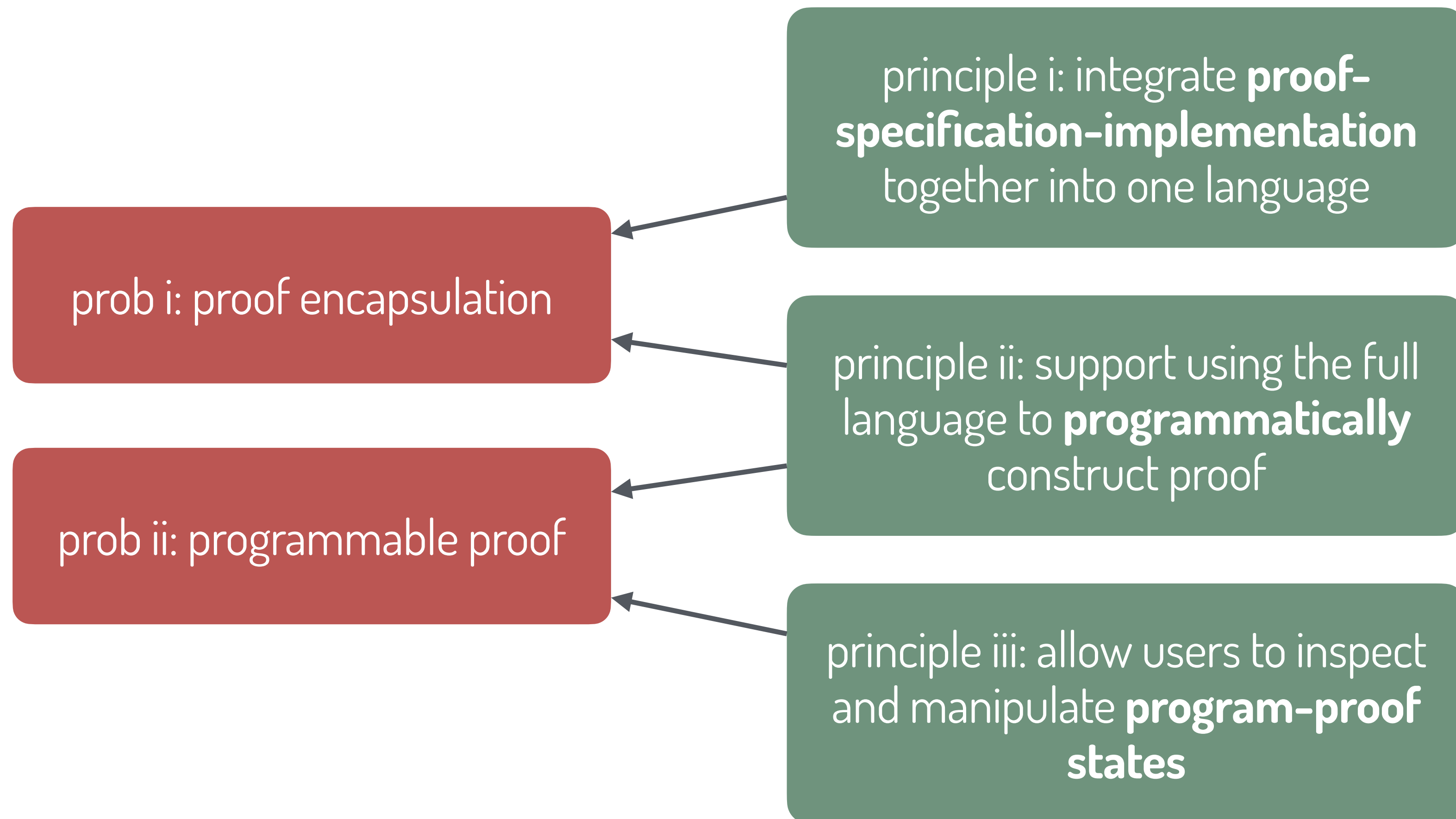
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 - ◎ use clangd for language server
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 - ◎ you own language-Star?

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for (; (order + 1) < pool->max_order; order++)
/*@ inv let p_i2 = (((integer) p) - __hyp_vmemmap) / 32 @*/
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/*@ inv let hyp_vmemmap = (pointer) __hyp_vmemmap @*/
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/*@ inv let V2 = each (integer i; start_i2 <= i && i < end_i2)
    {Owned<struct hyp_page>(hyp_vmemmap+(i*32)) } @*/
/*@ inv let p_page = V2.value[p_i2] @*/
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    buddy = __find_buddy_avail(pool, p, order);
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    p = min(p, buddy);
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}
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excerpts from the verified attach_page function in CN

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 - ongoing work: program-proof states reified as **local capabilities**

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